

St Lawrence Church of England Primary School
'Achieving together † Learning for life'

Written Calculation Policy

Pencil and paper procedures

Key Stages 1 and 2

Children progress through each stage as and when they are ready. For 'Age Related Expectation' (ARE) purposes, stage 1 = year 1, stage 2 = year 2 etc.

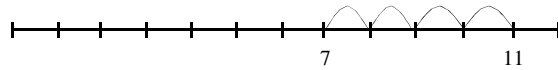
Addition

Stage 1

Number lines

Using objects and number lines to count on in ones

$$7 + 4 = 11$$



Progress from numbered lines to blank number lines (Teacher model number lines with missing numbers)

+ = signs and missing numbers

Use concrete objects and pictorial representations to solve problems such as:

$$\begin{array}{ll} 3 + 4 = & = 3 + 4 \\ 3 + \quad = 7 & 7 = \quad + 4 \\ + 4 = 7 & 7 = 3 + \quad \\ + \nabla = 7 & 7 = \quad + \nabla \end{array}$$

Stage 2

Partition into tens and ones and recombine

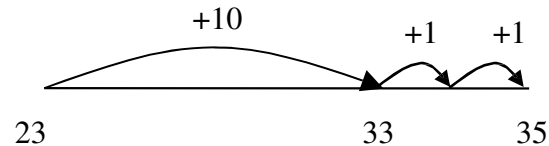
$$\begin{aligned} 12 + 23 &= 10 + 2 + 20 + 3 \\ &= 30 + 5 \\ &= 35 \end{aligned}$$

Also:

$$\begin{array}{l} \text{12} + \text{23} \\ \swarrow \quad \searrow \\ 10 + 20 + 2 + 3 = 30 + 5 = 35 \end{array}$$

refine to partitioning the second number only:

$$\begin{aligned} 23 + 12 &= 23 + 10 + 1 + 1 \\ &= 33 + 1 + 1 \\ &= 35 \end{aligned}$$



+ = signs and missing numbers

Continue using a range of equations as in Stage 1 but with appropriate, larger numbers.

Extend to:

$$14 + 5 = 10 +$$

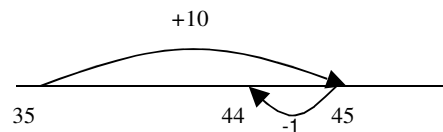
and adding three numbers:

$$32 + \quad + \quad = 100 \quad 35 = 1 + \quad + 5$$

Mental Method

Add 9 or 11 by adding 10 and adjusting by 1

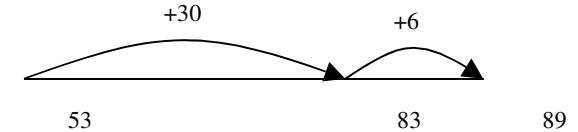
$$35 + 9 = 44$$



Stage 3

Partition into tens and ones and recombine Partition both numbers and recombine. Refine to partitioning the second number only e.g.

$$\begin{aligned} 36 + 53 &= 53 + 30 + 6 \\ &= 83 + 6 \\ &= 89 \end{aligned}$$



Add a near multiple of 10 to a two-digit number

Continue as in Stage 2 but with appropriate numbers e.g. $35 + 19$ is the same as $35 + 20 - 1$.

+ = signs and missing numbers

Continue using a range of equations as in Stages 1 and 2 but with appropriate, larger numbers

Pencil and paper procedures

$$83 + 42 = 125$$

Progress to units first:

$$\begin{array}{r} 80 + 3 \\ + 40 + 2 \\ \hline 120 + 5 = 125 \end{array} \quad \text{to} \quad \begin{array}{r} 83 \\ + 42 \\ \hline 125 \end{array}$$

Subtraction

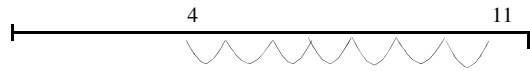
Stage1

Objects/Pictures / marks in Visual and practical activities

Sam spent 4p. What was his change from 10p?



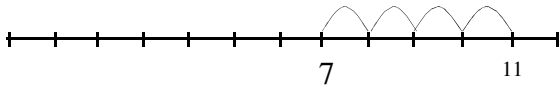
Number lines (numbered, progressing to empty)



$11 - 7 = 4$
Counting back

To reinforce concept: Practical strategies essential to see 'difference'.

Counting on to see the difference between 7 and 11



Recording by - drawing jumps on prepared lines
- constructing own lines

- = signs and missing numbers

Use concrete objects and pictorial representations to solve problems such as:

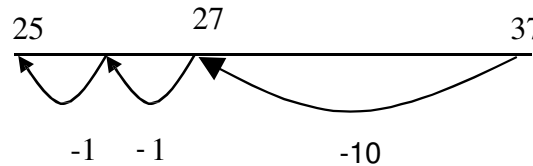
$$\begin{array}{ll} 7 - 3 = & = 7 - 3 \\ 7 - & = 4 & 4 = - 3 \\ - 3 = 4 & 4 = 7 - \\ - \nabla = 4 & 4 = - \nabla \end{array}$$

Stage2

Using concrete objects and pictorial representations

Use known number facts and place value to subtract
(partition second number only)

$$\begin{aligned} 37 - 12 &= 37 - 10 - 2 \\ &= 27 - 2 \\ &= 25 \end{aligned}$$



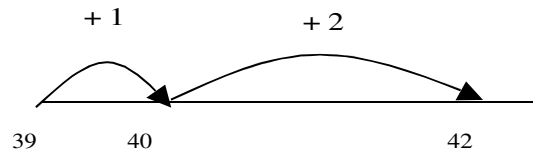
- = signs and missing numbers

Continue using a range of equations as in Stage1 but with appropriate numbers.

Extend to $14 + 5 = 20 -$

Find a small difference by counting up

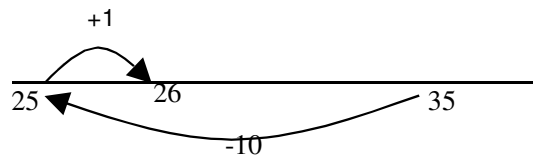
$$42 - 39 = 3$$



Mental Method

Subtract 9 or 11. Begin to add/subtract 19 or 21

$$35 - 9 = 26$$



Stage3

Find a small difference by counting up

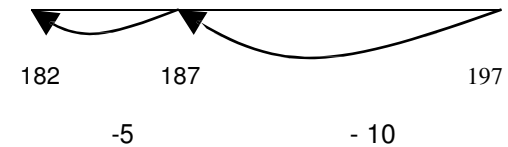
Continue as in Stage 2 but with appropriate numbers e.g.

$$102 - 97 = 5$$

Use known number facts and place value to subtract

Continue as in Stage 2 but with appropriate numbers e.g. 3 digit number - 2 digit number:

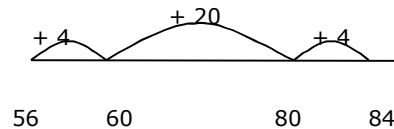
$$197 - 15 = 182$$



Pencil and paper procedures

Complementary addition:

$$84 - 56 = 28$$



Use expanded method as an introduction to decomposition:

$$\begin{array}{r} 90 \quad 2 \\ - 30 \quad 8 \\ \hline \end{array} \rightarrow \begin{array}{r} 80 \quad 12 \\ - 30 \quad 8 \\ \hline 50 + 4 = 54 \end{array}$$

Subtraction

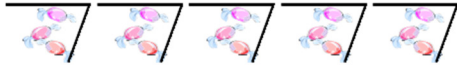
Stage 4	Stage 5	Stage 6
<p><u>Find a difference by counting up:</u></p> <p>e.g. $8006 - 2993 = 5013$</p> <p>This can be modelled on an empty number line</p> <p><u>Pencil and paper procedures</u></p> $\begin{array}{r} 8 \\ - 38 \\ \hline 54 \end{array}$	<p><u>Pencil and paper procedures</u></p> <p>Use decomposition</p> $\begin{array}{r} \\ \cancel{35}2 \\ - 178 \\ \hline 174 \end{array}$ <p>Extend to numbers with any number of digits and decimals with 1 and 2 decimal places.</p> <p>Extend to decomposition using '0' as a place holder</p>	<p><u>Pencil and paper procedures</u></p> <p>Practice and extend formal written methods of columnar addition with increasing large number to aid fluency.</p> <p>Practice mental calculations with increasingly large numbers.</p>

Multiplication

Stage 1

Pictures and symbols

There are 3 sweets in one bag.
How many sweets are there in 5 bags?



(Recording on a number line modelled by the teacher when solving problems)

Use of bead strings to model groups of numbers.

Arrays and repeated addition

$$\begin{array}{cccc} \bullet & \bullet & \bullet & \bullet \\ \bullet & \bullet & \bullet & \bullet \end{array} \quad 4 \times 2 \text{ or } 4 + 4$$

$$2 \times 4$$

Stage 2

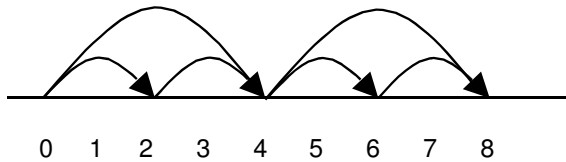
Arrays and repeated addition

$$\begin{array}{cccc} \bullet & \bullet & \bullet & \bullet \\ \bullet & \bullet & \bullet & \bullet \end{array} \quad 4 \times 2 \text{ or } 4 + 4$$

$$2 \times 4$$

or repeated addition:

$$2 + 2 + 2 + 2$$



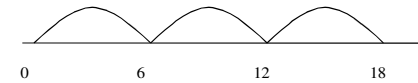
x = signs and missing numbers

$$\begin{array}{ll} 7 \times 2 = & = 2 \times 7 \\ 7 \times \quad = 14 & 14 = \quad \times 7 \\ \times 2 = 14 & 14 = 2 \times \quad \\ \times \nabla = 14 & 14 = \quad \times \nabla \end{array}$$

Stage 3

Number lines

$$3 \times 6$$



Arrays

$$6 \times 3$$

Partition

$$35 \times 2 = 70$$

x	30	5
2	60	10

$$60 + 10 = 70$$

Doubling multiples of 5 up to 50

$$15 \times 2 = 30$$

$$\begin{array}{l} \text{Partition: } (10 \times 2) + (5 \times 2) \\ 20 + 10 \\ = 30 \end{array}$$

x = signs and missing numbers

Continue using a range of equations as in Stage 2 but with appropriate numbers.

Multiplication

Stage 4

x = signs and missing numbers

Continue using a range of equations as in Stage 2 but with appropriate numbers

Pencil and paper procedures

Grid method:

TU x U

23 x 7 is approximately 20 x 10 = 200

23 x 7 = 161

	T	U
x	20	3
7	140	21

$$140 + 21 = 161$$

HTU x U

123 x 3 = 369

	H	T	U
x	100	20	3
3	300	60	9

$$300 + 60 + 9 = 369$$

Stage 5

x = signs and missing numbers

Continue using a range of equations as in Stage 2 but with appropriate numbers

Pencil and paper procedures

Move on to formal method when appropriate:

$$\begin{array}{r} 125 \\ \times \quad 7 \\ \hline 875 \\ 13 \\ \hline \end{array}$$

2741 x 6 becomes

$$\begin{array}{r} 2741 \\ \times \quad 6 \\ \hline 16446 \\ 42 \\ \hline \end{array}$$

Answer: 16 446

TU x TU

Grid method:

72 x 38 is approximately 70 x 40 = 2800

72 x 38 = 2736

$$\begin{array}{r|l|l} x & 70 & 2 \\ \hline 30 & 2100 & 60 \\ \hline 8 & 560 & 16 \\ \hline & 2736 & \\ \hline & & 1 \end{array} = 2160 + 576 = 2736$$

Estimate and check.

Stage 6

x = signs and missing numbers

Continue using a range of equations as in Stage 2 but with appropriate numbers

Pencil and paper procedures

'Carried' numbers to sit on top line of answer box

$$\begin{array}{r} 25 \\ \times \quad 17 \\ \hline 175 \\ 250 \\ \hline 425 \end{array}$$

Grid method

Estimate and check

372 x 24 is approximately 400 x 20 = 8000

$$\begin{array}{r|l|l|l} x & 300 & 70 & 2 \\ \hline 20 & 6000 & 1400 & 40 \\ \hline 4 & 1200 & 280 & 8 \\ \hline & & & 1488 \\ & & & + \\ & & & 8928 \end{array}$$

Move to formal multiplication method:

$$\begin{array}{r} 372 \\ \times \quad 24 \\ \hline 7440 \\ 14288 \\ \hline 8928 \end{array}$$

1

Division

Stage 1

Pictures / marks

12 children get into teams of 4 to play a game. How many teams are there?



Stage 2

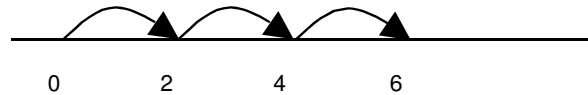
Understand division as sharing and grouping

Sharing – 6 sweets are shared between 2 people. How many do they have each?

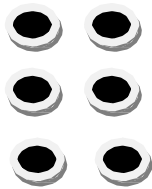


$6 \div 2$ can be modelled as:

Grouping – There are 6 sweets. How many people can have 2 each? (How many 2's make 6?)



Using objects in arrays -



Putting 6 objects into groups of two. How many groups?

\div = signs and missing numbers

$6 \div 2 =$	$= 6 \div 2$
$6 \div = 3$	$3 = 6 \div$
$\div 2 = 3$	$3 = \div 2$
$\div \nabla = 3$	$3 = \div \nabla$

Stage 3

\div = signs and missing numbers

Continue using a range of equations as in Stage 2 but with appropriate numbers.

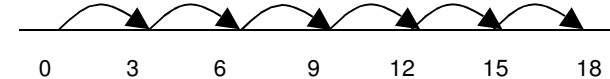
Understand division as sharing and grouping

$18 \div 3$ can be modelled as:

Sharing – 18 shared between 3 (see Stage 2 diagram)



Grouping - How many 3's make 18?



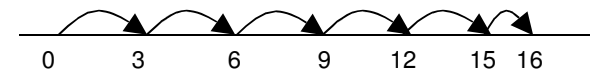
Also use arrays

Remainders

$16 \div 3 = 5 \text{ r}1$

Sharing - 16 shared between 3, how many left over?

Grouping – How many 3's make 16, how many left over?
e.g.



Division

Stage 4

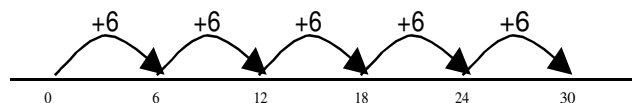
÷ = signs and missing numbers

Recall methods from Stage 2

Sharing and grouping

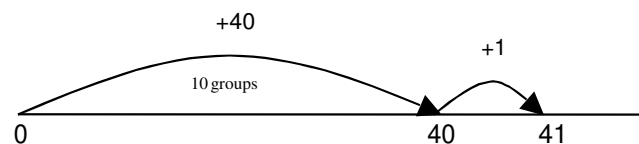
$30 \div 6$ can be modelled as:

grouping – groups of 6 taken away and the number of groups counted e.g.:



sharing – sharing among 4, the number given to each person

$$41 \div 4 = 10 \text{ r}1$$



OR $41 = (10 \times 4) + 1$

Stage 5

÷ = signs and missing numbers

Recall methods from Stages 3 and 4

Remainders

Quotients expressed as fractions or decimal fractions:

$$61 \div 4 = 15 \frac{1}{4} \text{ or } 15.25$$

Pencil and paper procedures

Use 'bus stop' method for division:

Estimate and check.

$$360 \div 8 \text{ is approximately } 400 \div 8 = 50$$

$$\begin{array}{r} 45 \\ 8 \overline{) 360} \end{array}$$

Extend to division of decimal numbers by a single digit, up to two decimal places:

$$\begin{array}{r} 078.33 \\ 3 \overline{) 22325.100} \end{array}$$

Stage 6

÷ = signs and missing numbers

Remainders

Quotients expressed as fractions or decimal fractions:

$$676 \div 8 = 84.5$$

Pencil and paper procedures

Estimate and check.

$$432 \div 15 \text{ is approximately } 450 \div 15 = 30$$

$$\begin{array}{r} 28 \text{ r}12 \\ 15 \overline{) 432} \\ \underline{30} \\ 132 \\ \underline{120} \\ 120 \\ \underline{120} \\ 0 \end{array}$$

Express remainders as fractions or as decimals:

$$\begin{array}{r} 28.8 \\ 15 \overline{) 432.0} \\ \underline{30} \\ 132 \\ \underline{120} \\ 120 \\ \underline{120} \\ 0 \end{array}$$